

## Section T-6 — Entropic Curvature Tensor R and Its Flow

*Bridge section between C-4 tensor dynamics and C-5 geometric manifold*

T-2 defined stability through the Stability Tensor  $T^{IJ}$ .

T-3 supplied the transport and evolution law that allows tensor structures to flow covariantly on the CUWF manifold.

T-5 built the Entanglement Tensor  $\Xi^{IJ}$  as curvature coherence generated from stability transport.

T-6 now introduces entropic curvature R as the final object in the chain:

$$T \rightarrow \Xi \rightarrow R \rightarrow \text{geometry evolves} \rightarrow \text{quantum emerges}$$

This section is intentionally concise. Its role is not to provide the full classification of CUWF geometry, but to establish the curvature object required before that classification can be developed. The full treatment of conifold behavior, sectional curvature, DOF-twist geometry, and singular-node structure belongs to C-5.

### T-6.1 Definition (Riemann-like Entropic Curvature)

The curvature tensor on the CUWF manifold is defined in Riemann-like form as:

$$R^{IJ}{}_{KL} = \partial^K \Gamma^{IJ}{}_{L} - \partial^L \Gamma^{IJ}{}_{K} + \Gamma^{IJ}{}_{M}{}^K \Gamma^{ML}{}_{J}{}^K - \Gamma^{IJ}{}_{M}{}^L \Gamma^{ML}{}_{J}{}^K \quad (18)$$

This tensor measures how the entropic connection  $\Gamma$  fails to remain flat when transported around the CUWF manifold. In ordinary geometric language, curvature records the nontrivial bending of a connection. In CUWF language, R records how collapse geometry, DOF structure, and mixed-sector tensor directions twist into quantum-active configurations.

Component	Effect
$\partial\Gamma$	Local deformation of collapse geometry.
$\Gamma\cdot\Gamma$	Nonlinear coupling; source of tunneling and entanglement activation.

Index ordering	Tracks DOF-twist, mode branching, and the orientation of curvature flow.
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The curvature condition is direct:

If  $R = 0$ , the geometry is flat: no tunneling and no entanglement are activated by curvature.

If  $R \neq 0$ , the geometry twists: quantum activation becomes possible.

Thus, in C-4, quantum behavior is not randomness. It is curvature becoming dynamically relevant.

### T-6.2 Ricci-like & Scalar Contractions

The full curvature tensor can be contracted into lower-order curvature measures that describe effective collapse geometry and global entropic tension.

Ricci-like contraction:

$$R_j^L = R^L_j \quad (19)$$

Scalar curvature:

$$R = g^{lj} R_{lj} \quad (20)$$

Tensor	Meaning
$R^L_j^K$	Full entropic geometry of the CUWF manifold.
$R_j^L$	Collapse-effective curvature after contraction.
$R$	Global entropic tension; scalar measure of curvature regime.

The sign of scalar curvature provides a compact regime indicator:

Curvature sign	Regime
$R > 0$	Collapse basin; classical behavior.
$R \approx 0$	Metastable plateau; threshold-sensitive behavior.
$R < 0$	Divergent geometry; tunneling regime.

Curvature therefore sets the quantum/classical ratio. Positive curvature supports ordinary basin collapse. Near-zero curvature marks a soft boundary. Negative curvature opens the geometry into instability, tunneling, or nonlocal propagation.

### T-6.3 Why Curvature Exists (Link Back to T-2 / T-3 / T-5)

Curvature does not appear as an independent decorative object. It is generated because the stability structure of CUWF evolves under a non-flat entropic connection.

Recall the Stability Tensor:

$$T^{IJ} = \nabla^I \nabla^J E + \Phi^{IJ}$$

When covariant derivatives fail to commute, the result is curvature:

$$[\nabla^I, \nabla^J] V^K = R^K_{L^IJ} V^L \quad (21)$$

This gives the structural chain:

Soft mode  $\rightarrow$  induces  $\Xi$ .

$\Xi \rightarrow$  induces R.

R  $\rightarrow$  propagates entanglement.

Geometry is therefore not passive in CUWF. It reacts to stability softening, stores the effect as curvature, and spreads correlation through the manifold. What standard quantum theory treats as nonlocal correlation is here interpreted as curvature response and propagation through the entropic tensor geometry.

### T-6.4 Curvature Flow Law (Preview of Paper C-5)

The evolution of the entropic curvature tensor may be written schematically as:

$$D_{\tau} R^{IJ} = -\nabla^I \nabla^J T^{KL} + \Gamma\text{-terms} + \text{nonlinear backreaction} \quad (22)$$

This is not yet the full C-5 geometric field theory. It is the bridge law showing how curvature responds to tensor instability and how that response becomes a propagating geometric process.

Process	Effect
T softens	Eigen-mode destabilizes.
$\Xi$ grows	Cross-node or cross-sector coupling strengthens.
R spreads	Quantum correlation propagates through curvature flow.

The result is the central transition of T-6: quantum behavior becomes curvature flow. It is not an extra probabilistic event added to the system; it is the evolution of the manifold after stability and entanglement have altered the connection geometry.

### T-6.5 Placement Note

This section is a bridge.

Its purpose is to introduce the entropic curvature tensor and show how it completes the chain from stability to entanglement to geometry. Full manifold geometry, sectional curvature, DOF-cone topology, conifold behavior, and singular node theory will be developed in C-5, the Geometry Volume.

Accordingly, T-6 should be read as the closing curvature layer of C-4 and as the opening doorway into C-5.

### T-6 Final Summary

T-6 establishes the following results:

R is the entropic curvature generated from instabilities in  $T^{\wedge}IJ$ .

Negative curvature corresponds to tunneling and nonlocal propagation.

Curvature evolves through tensor flow, not probability.

T-6 serves as the structural bridge from the tensor dynamics of C-4 to the full geometric expansion of C-5.

One-line essence:

Quantum emergence = curvature flow on the entropic manifold.