

## LEVEL 10 — Morphology Layer

Shape Descriptors, Collapse Geometry, Node Classification, and Multi-Scale Morphological Signatures

Level 10 introduces the morphology layer of the CUWF Mathematical Handbook. Where Level 6 describes collapse dynamics, Level 7 assembles the Master Equation architecture, and Levels 8–9 extend applications and auxiliary tools, Level 10 focuses on the visible and classifiable shapes produced by collapse. It is a geometry-recognition layer: it helps identify whether a collapse process forms a point, line, sheet, funnel, torus-like ring, surface deformation, or multi-center basin.

In this handbook, morphology does not replace dynamics. It reads the geometric signatures produced by dynamics. A collapse event is governed by the full-system CUWF evolution law

$$d\Omega/d\tau = -\nabla_{\mathcal{F}}G[\Omega]$$

and, in field-level pedagogical form, by

$$\partial\Psi/\partial\tau = -\delta G/\delta\Psi$$

Level 10 then asks: after or during this evolution, what shape has the collapse geometry produced?

### Notation Convention

$\Omega$  denotes the full CUWF state:  $\Omega(\tau) = \{X(\tau), g(\tau), \Xi_{\text{eff}}(\tau), N_{\text{eff}}(\tau)\}$ .

$\Psi(x, \tau)$  denotes a field-level or pedagogical representation of the collapse-wave component inside  $\Omega$ .

$\nabla\Psi$ ,  $\Delta\Psi$ , Hessian( $\Psi$ ), and related quantities are local shape diagnostics, not the full theory by themselves.

Morphology indicators classify geometric signatures; they do not prove the full physical interpretation unless connected back to  $G[\Omega]$ ,  $\Xi_{\text{eff}}$ ,  $R(N_{\text{eff}})$ , and curvature evolution.

### 10.1 Collapse Morphology — Shape Descriptor Equation

This subsection introduces a compact descriptor for recognizing local collapse shape. The purpose is not to replace the collapse equation, but to provide a quick diagnostic for whether a region is becoming point-like, sheet-like, or ring-like under collapse.

$$C\_shape(x) = |\nabla\Psi(x)| / (1 + \Psi(x)^2)$$

Condition / Quantity	Interpretation in CUWF morphology
High $ \nabla\Psi $	Steep local wave slope; collapse tends toward point-like compression or sharp ridges.
Low $ \nabla\Psi $ over a broad region	Collapse may form a sheet-like or basin-like morphology.
Ring-like gradient pattern	Collapse may produce torus-like or cavity-like morphology.
Large $\Psi$ denominator effect	Very high field amplitude can reduce the descriptor, preventing simple gradient magnitude from overclassifying a region.

**Interpretive note:**  $C\_shape(x)$  is best used as a first-pass shape detector. It should be cross-checked with Hessian structure, Laplacian signs, curvature response, and node classification.

### 10.2 Multi-Scale Spatial Patterns — Local vs Global Geometry

Collapse morphology often appears at multiple scales. A small collapse dent, a mesoscopic ridge, and a macroscopic basin may coexist in the same field. A wavelet-style decomposition separates these scale layers.

$$\Psi(x) = \sum_s \Psi_{-s}(x), \quad \Psi_{-s}(x) = \int \Psi(u) W_{-s}(x - u) du$$

Condition / Quantity	Interpretation in CUWF morphology
Small scale $s$	Micro-patterns such as fine dents, sharp local compressions, or early node seeds.
Medium scale $s$	Meso-patterns such as ridges, trenches, channels, or basin boundaries.
Large scale $s$	Macro-patterns such as global basins, broad deformations, or large collapse regions.

**Interpretive note:** This decomposition is morphological rather than dynamical. It helps identify where collapse has formed structures at different observational resolutions.

### 10.3 Spatial Collapse Regions — Contraction Mapping Formula

A collapse process can be interpreted as a map from an initial geometry to a post-collapse geometry. The Jacobian of that map indicates whether local volume contracts, expands, or nearly degenerates.

$$K(x) = 1 - \det(J_\Psi(x))$$

Condition / Quantity	Interpretation in CUWF morphology
$\det(J_\Psi) < 1$	The local region contracts under the collapse map.
$\det(J_\Psi) > 1$	The local region expands or opens.
$\det(J_\Psi) \approx 0$	The region nearly collapses into a line, sheet, or point-like structure.
$K(x)$ large	Strong contraction signature; possible node, funnel, or topology-sensitive region.

**Interpretive note:**  $K(x)$  should be interpreted as a contraction indicator. In a full CUWF model, extreme contraction must be checked against curvature regulation and  $N_{eff}$  response.

### 10.4 Geometric Commitment Structures — Irreversibility Marker

Some morphological features remain flexible, while others become locked into the geometry. A commitment marker estimates whether neighboring field values are sharply separated at infinitesimal scale.

$$\Gamma_{\text{commit}}(x) = \lim_{\delta \rightarrow 0} |\Psi(x) - \Psi(x + \delta)|$$

Condition / Quantity	Interpretation in CUWF morphology
High $\Gamma_{\text{commit}}(x)$	Geometry is sharply locked; local reversal becomes difficult.
Low $\Gamma_{\text{commit}}(x)$	Geometry remains flexible or weakly differentiated.
Persistent high $\Gamma_{\text{commit}}$	Possible irreversible ridge, boundary layer, or post-collapse structural memory.

**Interpretive note:** The symbol  $\Gamma_{\text{commit}}$  is used here to avoid confusion with Christoffel symbols  $\Gamma^{k}_{ij}$ . It is a morphology marker, not a connection coefficient.

### 10.5 Entropic Pathway Geometry — Path Curve Descriptor

Collapse often leaves directional traces. These traces can be represented as curves  $L$  parameterized by  $s$ . The curvature of the path indicates whether collapse travels straight, bends, or twists.

$$x = x(s), \quad \mathbf{K}_L = |x' \times x''| / |x'|^3$$

Condition / Quantity	Interpretation in CUWF morphology
$\mathbf{K}_L \approx 0$	Collapse pathway is nearly straight.
$\mathbf{K}_L$ high	Collapse route bends strongly.
Rapidly changing $\mathbf{K}_L$	Possible torsion, swirl, or instability along the collapse channel.

**Interpretive note:** Path curvature does not define the collapse force. It describes the shape of the path left by collapse under entropic drift, geometry, and kernel coupling.

### 10.6 Node Morphology — Node Classification Formula

Collapse nodes can take several geometric forms. A classification rule compares local derivative signatures to identify whether a node is line-like, sheet-like, point-like, or ring/torus-like.

$$N\_type = \operatorname{argmax} \{ |\partial_i \Psi|, |\partial_i \partial_j \Psi|, |\nabla \Psi|, |\Delta \Psi| \}$$

Condition / Quantity	Interpretation in CUWF morphology
Dominant $ \partial_i \Psi $	Line-node or directional ridge signature.
Dominant $ \partial_i \partial_j \Psi $	Sheet-node or surface deformation signature.
Dominant $ \nabla \Psi $	Point-node or sharp localized collapse signature.
Dominant $ \Delta \Psi $	Ring, cavity, or torus-like morphology candidate.

**Interpretive note:** This rule is a practical classifier. In final analysis, node identity should be validated with curvature, topology, and stability diagnostics.

### 10.7 Multi-Center Interaction — Geometry of Combined Fields

When multiple collapse centers coexist, their fields combine. The resulting morphology may form neutral zones, saddle regions, competing basins, or merged nodes.

$$\Psi_{total}(x) = \sum_k \Psi_{k}(x), \quad \nabla \Psi_{total}(x) \approx 0, \quad \lambda_1 \cdot \lambda_2 < 0$$

Condition / Quantity	Interpretation in CUWF morphology
$\nabla \Psi_{total} \approx 0$	Neutral or balance region between collapse centers.
$\lambda_1 \cdot \lambda_2 < 0$	Mixed Hessian signs; saddle-like geometry.
Overlapping $\Psi_k$	Possible basin merging, interference, or collapse competition.

**Interpretive note:** Multi-center morphology is especially useful for interpreting clustered collapse, entangled nodes, and basin competition.

### 10.8 Collapse Surfaces — Surface Morphology Formula

Some collapse processes deform surfaces rather than isolated points. If a surface  $S$  is defined by  $f(x) = 0$ , normal curvature estimates how strongly collapse deforms that surface.

$$K_n = n^T H_f n$$

Condition / Quantity	Interpretation in CUWF morphology
High $K_n$	Strong surface-level deformation along the normal direction.
Low $K_n$	Gentle or weak deformation.
Mixed surface curvature	Possible saddle-like or folded collapse surface.

**Interpretive note:**  $K_n$  is a local surface diagnostic. It should be read together with entropic curvature and collapse-stability information.

### 10.9 Collapse Funnels — Funnel Profile Equation

A collapse funnel is a localized geometry where the field sinks sharply near a center and gradually flattens outward. A simple radial profile provides a readable prototype.

$$\Psi(r) \approx -A / (1 + r^2)$$

Condition / Quantity	Interpretation in CUWF morphology
$r \approx 0$	Center of the funnel; strongest collapse depth.
$A$ large	Deep collapse funnel.
Large $r$	Profile flattens; collapse influence weakens outward.

**Interpretive note:** This formula is a prototype profile, not a universal law. Real CUWF funnels may include anisotropy, entanglement distortion, and curvature regulation.

### 10.10 Hierarchical Contraction Map — Multi-Level Geometry

Collapse morphology may be layered. Micro dents, meso ridges, and macro basins can be combined into a hierarchical contraction map.

$$\mathcal{H}(x) = \sum_l w_l C_l(x)$$

Condition / Quantity	Interpretation in CUWF morphology
$l = 1$	Micro dents or small-scale collapse signatures.
$l = 2$	Meso ridges, trenches, or channels.
$l = 3$	Macro basins, global deformation, or large-scale collapse topology.
$w_l$	Weight controlling how strongly level $l$ contributes to the total morphology map.

**Interpretive note:** A hierarchical map is useful for visualizing how local collapse signatures aggregate into larger geometric structures.

### 10.11 Summary — What the Level 10 Equations Achieve

Level 10 provides the morphology-recognition layer of the CUWF Mathematical Handbook. Its equations do not duplicate collapse dynamics, the Master Equation, or the extended operator library. Instead, they classify the geometric forms produced by those deeper mechanisms.

Level 6 describes how collapse evolves; Level 10 describes the shapes collapse leaves behind.

Level 7 integrates collapse, curvature, entanglement, and dimensional flow; Level 10 provides geometric labels and descriptors for those results.

Level 8 applies CUWF to physical domains; Level 10 supplies morphology tools that help interpret those application regimes.

Level 9 extends the mathematical toolbox; Level 10 specializes that toolbox for shape recognition and geometric classification.

Level 11 will continue from morphology into entropic curvature mechanics, where the shapes identified here acquire curvature dynamics.

**The central result of Level 10 is:** collapse morphology can be analyzed through shape descriptors, scale decomposition, contraction maps, commitment markers, path curvature, node classifiers, surface curvature, funnel profiles, and hierarchical contraction maps. These tools allow CUWF to identify, classify, and compare collapse geometry across micro-, meso-, and macro-scales.

### Level 10 Practical Cautions

Morphology indicators are diagnostic tools, not complete dynamical laws. They must be connected back to  $d\Omega/d\tau = -\nabla_{\mathcal{F}}G[\Omega]$ .

$\Psi$ -based formulas are field-level descriptions. The full CUWF state remains  $\Omega = \{X, g, \Xi_{\text{eff}}, N_{\text{eff}}\}$ .

High gradients or high curvature do not automatically mean physical singularity; CUWF requires checking  $N_{\text{eff}}$  regulation,  $\Xi_{\text{eff}}$  coupling, and curvature flow.

Node classification is convention-sensitive. The sign conventions for  $\Delta\Psi$ , Hessian eigenvalues, and curvature must be stated before comparing simulations.

Prototype profiles such as  $\Psi(r) \approx -A/(1+r^2)$  are illustrative; full simulations may require anisotropic, nonlocal, or topology-aware forms.