

## LEVEL 19 — Geometric Simulation Tools

Level 19 introduces the geometry-based simulation layer of the CUWF Mathematical Handbook. Levels 16–18 established nonlinear solution methods, real-space numerical engines, and spectral methods. Level 19 adds a geometric view: the CUWF field is treated not only as an array of values or a spectrum of modes, but also as a deforming manifold whose surface, curvature, topology, and entanglement-induced distortions can be simulated directly.

In the official full-system notation of CUWF, the universe-state is represented as  $\Omega(\tau)$ , and the dynamical law is written as:

$$d\Omega/d\tau = -\nabla_{\mathcal{F}G}[\Omega]$$

The stationary or admissible projection condition is:

$$\nabla_{\mathcal{F}G}[\Omega] = 0$$

For computational and pedagogical purposes, Level 19 often works with the field-level projection

$\Psi(x, \tau)$ :

$$\partial\Psi/\partial\tau = -\delta_G/\delta\Psi$$

Thus,  $\Psi$  should be read as a field-level representation or computational slice of the full CUWF state  $\Omega$ , not as the whole universe-state by itself.

### 19.1 The CUWF Manifold as a Dynamic Geometry

#### What it is

A CUWF simulation can represent  $\Psi(x, \tau)$  as a scalar field, but Level 19 also represents it as a deforming geometric hypersurface. This allows collapse funnels, ridges, sheets, and curvature pockets to be visualized as shape changes rather than only as numerical field values.

#### What it is used for

Visualizing collapse funnels and collapse ridges.

Tracking curvature propagation across the entropic manifold.

Detecting geometric instabilities before collapse localization.

Capturing entanglement-induced bending or nonlocal geometric distortion.

### Core formulas

$$\Gamma(\tau): x \mapsto \Psi(x, \tau)$$

$$n = \nabla \Psi / |\nabla \Psi|$$

$$H \approx \nabla \cdot (\nabla \Psi / |\nabla \Psi|)$$

### Interpretation

The normal vector  $n$  describes the local direction of the surface, while  $H$  gives an approximate mean-curvature indicator. In a visualization, inward curvature flow corresponds to collapse-like contraction; outward flow corresponds to expansion or post-collapse redistribution.

## 19.2 Geometric Ricci-Type Flow Simulation

CUWF curvature may be simulated through a Ricci-type update modified by entropic and entanglement contributions. This is not identical to classical Ricci flow; it is a computational template for evolving geometry under CUWF-specific curvature response.

### Numerical geometry update

$$g_{ij}^{n+1} = g_{ij}^n - 2\Delta\tau (R_{ij}^{\wedge}(E) + \lambda E_{ij})$$

where  $R_{ij}^{\wedge}(E)$  is the entropic Ricci tensor and  $E_{ij}$  is the entanglement-induced geometric distortion tensor or its simulation analogue.

### Purpose

Smooth unwanted curvature spikes.

Identify attractor-like geometric configurations.

Simulate curvature breathing cycles.

Track whether collapse geometry relaxes, sharpens, or bifurcates.

## Interpretation

This approach creates a geometry-first simulation pathway. Instead of only updating  $\Psi$  as a scalar field, the simulation updates the metric-like structure that determines how future collapse and entropic drift will proceed.

### 19.3 Curvature Propagation Solver

#### What it is

A curvature propagation solver evolves the entropic curvature field  $\mathcal{R}_E$  as its own computational object. This is useful when curvature behaves like a propagating or redistributing field rather than a static by-product of  $\Psi$ .

#### Prototype curvature equation

$$\partial \mathcal{R}_E / \partial \tau = A \Delta \mathcal{R}_E - B \Delta^2 \mathcal{R}_E + C \Xi + D \epsilon \cdot \nabla \mathcal{R}_E$$

#### Numerical update

$$\mathcal{R}_E^{n+1} = \mathcal{R}_E^n + \Delta \tau F_{\text{curv}}(\mathcal{R}_E^n, \Psi^n, \epsilon^n)$$

#### What it is used for

Tracking curvature waves and curvature relaxation.

Detecting collapse precursors before sharp localization occurs.

Mapping stability basins in geometry space.

Studying curvature-resonance phenomena and breathing cycles.

#### Interpretation

The coefficients A, B, C, and D are model parameters. They should not be treated as universal constants unless specified by a particular CUWF solver model.

## 19.4 Geometric Entanglement Mapping

### What it is

Geometric entanglement mapping converts a nonlocal entanglement kernel into a geometric influence field. Instead of treating entanglement only as an abstract coupling matrix, the method visualizes how one region of the manifold pulls, twists, or biases another.

### Prototype kernel

$$K_{\text{ent}}(x,y) = \Xi(x)\Xi(y)e^{(-\alpha|x-y|)}$$

### Geometric influence field

$$E_{\text{geom}}(x) = \int K_{\text{ent}}(x,y)n(y)dS_y$$

### What it is used for

Tracking nonlocal geometric influence between regions.

Visualizing entanglement-induced bending.

Detecting nonlocal collapse synchrony.

Estimating when two collapse regions behave as a coupled geometric system.

### Interpretation

In the full  $\Omega$ -form, this role belongs to  $\Xi_{\text{eff}}$ . The kernel  $K_{\text{ent}}(x,y)$  and field  $\Xi(x)$  are field-level or model-level representations used to make  $\Xi_{\text{eff}}$  computable in simulations.

## 19.5 Topological Transition Detection

### What it is

Topological transition detection identifies regions where collapse geometry may change its qualitative structure: for example, from sheet-like to funnel-like, from a channel to a node, or from a continuous surface to a disconnected basin.

### Prototype topological indicator

$$T(x) = |\nabla\Psi|^{-1} |\mathcal{R}_E|$$

## Algorithm

Monitor  $T(x, \mathbf{T})$  during evolution.

Mark regions as critical when  $T$  exceeds a chosen threshold.

Refine the simulation mesh locally near critical regions.

Continue evolution and track whether topology actually changes.

## Interpretation

A high value of  $T(x)$  does not prove topology change by itself. It marks a candidate region requiring further geometric, spectral, and stability checks.

## 19.6 Entropic Flow Lines

### What it is

Entropic flow lines trace the paths followed by entropy-driven motion across the CUWF manifold. They help reveal collapse pathways, attractor basins, and drift channels.

### Entropic velocity field

$$v_E = -\nabla S$$

### Flow-line ODE

$$dx/d\mathbf{T} = v_E(x)$$

### What it is used for

Tracking information-flow and collapse-flow directions.

Visualizing collapse pathways and drift channels.

Identifying sinks, sources, and attractor structures.

Comparing entropy-driven motion with curvature-driven geometry changes.

## Interpretation

These flow lines are not ordinary particle trajectories. They are geometric diagnostics of entropic drift within a chosen CUWF model.

## 19.7 Stability Landscape Geometry

### What it is

Stability landscape geometry visualizes stability as a surface. The method treats the stability potential  $V_s$  as a height field over configuration or spatial coordinates.

### Prototype stability potential

$$V_s(\Psi) = f(\Xi, \mathcal{R}_E, \epsilon)$$

### Extruded surface

$$\Sigma = \{(x, V_s(x))\}$$

### What it is used for

Detecting metastable pockets.

Visualizing collapse pathways.

Mapping stability ridges and transition saddles.

Comparing curvature-stability and entanglement-stability coupling.

### Interpretation

The surface  $\Sigma$  is a visualization of stability structure, not the physical manifold itself. It should be interpreted as a diagnostic layer built on top of the CUWF state.

## 19.8 Curvature–Entanglement Coupled Simulation

### What it is

A coupled simulation evolves  $\Psi$ , curvature, entanglement, and geometry together. This is necessary because in CUWF each component modifies the others.

### Simulation cycle

Update  $\Psi$  using the field-level Master Equation or a solver approximation.

Compute  $\mathcal{R}_E$  from  $\Psi$ ,  $\epsilon$ , and geometric data.

Compute  $\Xi$  or a model approximation to  $\Xi_{\text{eff}}$ .

Update the geometric embedding  $\Gamma$  and/or metric  $g_{ij}$ .

Recompute geometric operators such as  $\Delta_E$ , normals, and curvature indicators.

Repeat until convergence, instability, attractor formation, or specified  $\tau_{\text{end}}$ .

### Interpretation

This feedback loop is the computational version of the CUWF coupling principle: collapse affects geometry, geometry affects entanglement, entanglement affects future collapse, and the full state evolves as  $\Omega$ .

## 19.9 Mesh Adaptation for Collapse Regions

### What it is

Mesh adaptation changes spatial resolution according to curvature, collapse intensity, or entanglement complexity. Regions with sharp curvature or strong collapse require finer resolution than flat regions.

### Prototype rule

if  $|\mathcal{R}_E| > \text{threshold}$ :  $\Delta x_{\text{new}} = \Delta x_{\text{old}} / 2$

### Operational rules

Refine mesh near curvature spikes, collapse funnels, and topological candidates.

Keep coarse mesh in stable, flat, or low-information regions.

Merge or coarsen adaptively to conserve memory and computation time.

Recompute operators after mesh adaptation to avoid inconsistent derivatives.

### Interpretation

Adaptive mesh refinement is a numerical strategy, not a CUWF physical law. Its role is to prevent the solver from missing sharp geometric events.

## 19.10 Geometry-Based Visualization Tools

### What it is

Geometry-based visualization converts CUWF simulation data into interpretable geometric objects. This is essential because many CUWF effects are structural: basins, ridges, funnels, stability pockets, and nonlocal geometric links.

### Visualization outputs

Curvature heatmaps.

Entanglement vector fields.

Surface normals and collapse ridges.

Stability landscape 3D plots.

Topological event markers.

Geodesic deformation maps.

Evolution movies across entropic time  $\tau$ .

### Interpretation

Visual outputs should be paired with numerical diagnostics. A visually interesting funnel, ridge, or bridge is not automatically a validated CUWF prediction unless supported by the relevant curvature, stability, and entanglement measures.

### 19.11 Summary of Level 19 Tools

Level 19 adds the geometric simulation layer to the CUWF Mathematical Handbook. It does not replace the real-space engine of Level 17 or the spectral tools of Level 18. Instead, it provides a geometric interpretation layer that treats collapse, curvature, topology, and entanglement as shape-changing processes on an entropic manifold.

Tool	Main Function
Dynamic manifold geometry	Represents $\Psi$ as a deforming hypersurface.
Ricci-type geometry flow	Updates geometry through entropic curvature and entanglement distortion.
Curvature propagation solver	Tracks curvature waves, spikes, and relaxation.

Geometric entanglement mapping	Converts nonlocal kernels into geometric influence fields.
Topological transition detection	Marks candidate topology-change regions.
Entropic flow lines	Visualizes drift, collapse pathways, and attractor basins.
Stability landscape geometry	Maps metastable pockets, ridges, and transition paths.
Adaptive mesh refinement	Improves resolution near collapse or curvature-critical zones.
Visualization suite	Produces maps, surfaces, vectors, and movies for interpretation.

Level 19 prepares the final computational layer: Level 20 — Full CUWF Computational Framework, where nonlinear solvers, real-space numerics, spectral methods, geometric simulation, diagnostics, and visualization are assembled into one integrated CUWF engine.

### Level 19 Practical Cautions

Geometric simulation is diagnostic and computational; it does not replace the full-system  $\Omega$ -form equation.

$\Psi$ -surface visualizations are projections of  $\Omega$ , not the entire CUWF universe-state.

High curvature, topological indicators, and visual funnels are candidate signals; they require stability and spectral verification.

Entanglement maps such as  $K_{ent}(x,y)$  are model-level approximations of  $\Xi_{eff}$ , not automatically equivalent to standard quantum entanglement.

Adaptive refinement and visualization can reveal structure, but they can also introduce numerical artifacts if not paired with convergence testing.